Representing and Reasoning about Web Access Control Policies

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Abstract—The advent of emerging technologies such as Web services, service-oriented architecture, and cloud computing has enabled us to perform business services more efficiently and effectively. However, we still suffer from unintended security leakages by unauthorized services while providing more convenient services to Internet users through such a cutting-edge technological growth. Furthermore, designing and managing Web access control policies are often error-prone due to the lack of logical and formal foundation. In this paper, we attempt to introduce a logic-based policy management approach for Web access control policies especially focusing on XACML (eXtensible Access Control Markup Language) policies, which have become the de facto standard for specifying and enforcing access control policies for various applications and services in current Web-based computing technologies. Our approach adopts Answer Set Programming (ASP) to formulate XACML that allows us to leverage the features of ASP solvers in performing various logical reasoning and analysis tasks such as policy verification, comparison and querying. In addition, we propose a policy analysis method that helps identify policy violations in XACML policies accommodating the notion of constraints in role-based access control (RBAC). We also discuss a proof-of-concept implementation of our method called XACML2ASP with the evaluation of several XACML policies from real-world software systems.

Keywords—XACML; Role-based Access Control; Answer Set Programming

I. INTRODUCTION

With the explosive growth of Web applications and Web services deployed on the Internet, the use of a policy-based approach has received considerable attention to accommodate the security requirements covering large, open, distributed and heterogeneous computing environments. Policy-based computing handles complex system properties by separating policies from system implementation and enabling dynamic adaptability of system behaviors by changing policy configurations without reprogramming the systems. In the era of distributed, heterogeneous and Web-oriented computing, the increasing complexity of policy-based computing demands strong support of automated reasoning techniques. Without analysis, most benefits of policy-based techniques and declarative policy languages may be in vain.

XACML (eXtensible Access Control Markup Language) [29], which is an XML-based language standardized by the Organization for the Advancement of Structured Information Standards (OASIS), has been widely adopted to specify access control policies for various Web applications. With expressive policy languages such as XACML, assuring the correctness of policy specifications becomes a crucial yet challenging task. Especially, identifying inconsistencies and differences between policy specifications and their expected functions is critical since the correctness of the implementation and enforcement of policies heavily relies on the policy specification. Due to its flexibility, XACML has been extended to support specialized access control models. In particular, XACML profile for role-based access control (RBAC) [4] provides a mapping between RBAC and XACML. However, the current RBAC profile does not support constraints that are an important element to govern all other elements in RBAC. In RBAC, permissions of specific actions on resources are assigned to authorized users with the notion of roles and such assignments are constrained with specific RBAC constraints. XACML-based RBAC policies are written to specify such assignments and corresponding rules, yet security leakage may occur in specifying XACML-based RBAC policies without having appropriate constraints in place. Furthermore, designing and managing such Web access control policies are often error-prone due to the lack of logical and formal foundation.

In this paper, we propose a systematic method to represent XACML policies in answer set programming (ASP), a declarative programming paradigm oriented towards combinatorial search problems and knowledge intensive applications. Compared to a few existing approaches to formalizing XACML policies, such as as [10], [16], our formal representation is more straightforward and can cover more XACML features. Furthermore, translating XACML to ASP allows us to leverage off-the-shelf ASP solvers for a variety of analysis services such as policy verification, comparison and querying. In addition, in order to support reasoning about role-based authorization constraints, we introduce a general specification scheme for RBAC constraints along with a policy analysis framework, which facilitates the analysis of constraint violations in XACML-based RBAC policies. The expressivity of ASP, such as ability to handle default reasoning and represent transitive closure, helps manage XACML and RBAC constraints that cannot be handled in other logic-based approaches [16]. We also overview our tool XACML2ASP and conduct experiments with real-world
XACML policies to evaluate the effectiveness and efficiency of our solution.

The rest of this paper is organized as follows. We give an overview of XACML, RBAC and ASP in Section II. In Section III, we show how XACML can be turned into ASP and how XACML analysis can be carried out using ASP solvers. We address XACML-based RBAC policy analysis in Section IV. Section V presents the system XACML2ASP along with experiments. We overview the related work in Section VI. Section VII concludes this paper with the future work.

II. BACKGROUND TECHNOLOGIES

A. eXtensible Access Control Markup Language

XACML has become the de facto standard for describing access control policies and offers a large set of built-in functions, data types, combining algorithms, and standard profiles for defining application-specific features. The root of all XACML policies is a policy or a policy set. A policy set is composed of a sequence of policies or other policy sets along with a policy combining algorithm and a target. A policy represents a single access control policy expressed through a target, a set of rules and a rule combining algorithm. The target defines a set of subjects, resources and actions the policy or policy set applies to. For applicable policy sets and policies, the corresponding targets should be true; otherwise, the policy set or policy yields no decision on the request. A rule set is a sequence of rules. Each rule in turn consists of a target, a condition, and an effect. The target of a rule has a similar structure as the target of a policy or a policy set, and decides whether the request is applicable to the rule. The condition is a Boolean expression to specify restrictions on the attributes in the target and refines the applicability of the rule and the effect is either one of “permit,” “deny,” or “indeterminate.” If a request satisfies both the target and condition of a rule, the response is sent with the decision specified by the effect element in the applicable rule. Otherwise, the response yields “notApplicable” which is typically considered as “deny.” Also, an XACML policy description often has conflicting rules, policies or policy sets, which are resolved by four different combining algorithms [29]: “Permit-overrides,” “Deny-Overrides,” “First-Applicable,” and “Only-One-Applicable.”

- Permit-Overrides: If there is any applicable rule that evaluates to permit, then the decision is permit. Otherwise, the decision is notApplicable.
- Deny-Overrides: If there is any applicable rule that evaluates to deny, then the decision is deny. Otherwise, the decision is notApplicable.
- First-Applicable: The decision is the effect of the first applicable rule in the listed order. If there is no applicable rule, then the decision is notApplicable.
- Only-One-Applicable: If more than one rule is applicable, then the decision is indeterminate. If there is only one applicable rule, then the decision is that of the rule. If no rule is applicable, then the decision is notApplicable.

Note that “Only-One-Applicable” combining algorithm is defined only for policy sets.

Consider an example XACML policy for a software development company, which is utilized throughout this paper, shown in Figure 1. Figure 2 gives a tree structure of this example policy. The root policy set \( p_3 \) contains two policies \( p_1 \) and \( p_2 \) which are combined using first-applicable combining algorithm. The policy \( p_1 \), which is the global
B. Role-based Access Control

RBAC is a widely accepted alternative to traditional mandatory access control (MAC) and discretionary access control (DAC) [24]. As MAC is used in the classical defense arena, the access is based on the classification of objects such as security clearance [23] while the main idea of DAC is that the owner of an object has the discretion over who can access the object [15], [22]. However, RBAC is based on the role of the subjects and can specify security policy in a way that maps to an organizational structure. A general family of RBAC models called RBAC96 was proposed by Sandhu et al. [21]. Intuitively, a user is a human being or an autonomous agent, a role is a job function or job title within the organization with some associated semantics regarding the authority and responsibility conferred on the user assigned to the role, and a permission is an approval of a particular mode of access to one or more objects in the system or some privileges to carry out specified actions.

Roles are organized in a partial order \( \geq \), so that if \( x \geq y \) then a role \( x \) inherits the permissions of a role \( y \). Therefore, members of a role \( x \) are also implicitly members of a role \( y \). In addition, RBAC introduces constraints that are a powerful mechanism for laying out higher-level organizational policies. Separation of duty (SoD) is a well-known principle for preventing fraud by identifying conflicting roles and has been studied in considerable depth by RBAC community [2], [7], [17]. SoD constraints in RBAC can be divided into Static SoD constraints, Dynamic SoD constraints and Historical SoD constraints. Static SoD constraints typically require that no user should be assigned to conflicting roles. Dynamic SoD constraints—with respect to activated roles in sessions—typically require that no user can activate conflicting roles simultaneously. Historical SoD constraints restrict the assignment and activation of conflicting roles over the course of time.

C. Answer Set Programming

ASP [20], [18] is a recent form of declarative programming that has emerged from the interaction between two lines of research—nonmonotonic semantics of negation in logic programming and applications of satisfiability solvers to search problems. The idea of ASP is to represent the search problem we are interested in as a logic program whose intended models, called “stable models (a.k.a. answer sets),” correspond to the solutions of the problem, and then find these models using an answer set solver—a system for computing stable models. Like other declarative computing paradigms, such as SAT (Satisfiability Checking) and CP (Constraint Programming), ASP provides a common basis for formalizing and solving various problems, but is distinct from others such that it focuses on knowledge representation and reasoning: its language is an expressive nonmonotonic language based on logic programs under the stable model semantics [11], [9], which allows elegant representation of several aspects of knowledge such as causality, defaults, and incomplete information, and provides compact encoding of complex problems that cannot be translated into SAT and CP [19]. As the mathematical foundation of answer set programming, the stable model semantics was originated from understanding the meaning of negation as failure in Prolog, which has the rules of the form

\[
a_1 \leftarrow a_2, \ldots, a_m, \not a_{m+1}, \ldots, \not a_n
\]

where all \( a_i \) are atoms and \( \not \) is a symbol for negation as failure, also known as default negation. Intuitively, under the stable model semantics, rule (1) means that if you have generated \( a_2, \ldots, a_m \) and it is impossible to generate any of \( a_{m+1}, \ldots, a_n \) then you may generate \( a_1 \). This explanation seems to contain a vicious cycle, but the semantics are carefully defined in terms of fixpoint.

While it is known that the transitive closure (e.g., reachability) cannot be expressed in first-order logic, it can be handled in the stable model semantics. Given the fixed extent of edge relation, the extent of reachable is the transitive
A. Abstracting XACML Policy Components

We consider a subset of XACML that covers more constructs than the ones considered in [28] and [16]. We allow the most general form of Target, take into account Condition, and cover all four combining algorithms.

XACML components can be abstracted as follows: Attributes are the names of elements used by a policy. Attributes are divided into three categories: subject attributes, resource attributes and action attributes. In the example policy above, developer, tester and employee are subject attributes; read and change are action attributes; codes is a resource attribute. A Target is a triple \(<Subjects, Resources, Actions>\). A Condition is a conjunction of comparisons. An Effect is either “permit,” “deny,” or “indeterminate.”

- An XACML rule can be abstracted as
  \(<\text{RuleID}, \text{Effect}, \text{Target}, \text{Condition}>\)
  where RuleID is a rule identifier. For example, rule \(r_1\) in Figure 1 can be viewed as
  \(<r_1, \text{permit}, \langle employee, read \lor \text{change}, \text{codes} \rangle, 8 \leq \text{time} \leq 17>\).

- An XACML policy can be abstracted as
  \(<\text{PolicyID}, \text{Target}, \text{Combining Algorithm}, \langle r_1, \ldots, r_n \rangle>\)
  where PolicyID is a policy identifier, \(r_1, \ldots, r_n\) are rule identifiers and Combining Algorithm is either permit–overrides, deny–overrides, or first–applicable. For example, policy \(p_1\) in Figure 1 is abstracted as:
  \(<p_1, \text{Null}, \text{permit–overrides}, \langle r_1, r_2 \rangle>\).

- Similarly we can abstract an XACML policy set as
  \(<\text{PolicySetID}, \text{Target}, \text{Combining Algorithm}, \langle p_{m_1}, \ldots, p_{m_n}, p_{s_{m+1}}, \ldots, p_{s_n} \rangle>\)
  where PolicySetID is a policy set identifier, \(p_{m_1}, \ldots, p_{m_n}\) are policy identifiers, \(p_{s_{m+1}}, \ldots, p_{s_n}\) are policy set identifiers, and Combining Algorithm is either permit–overrides, deny–overrides, first–applicable, or only–one–applicable. For example, policy set \(p_{s_1}\) can be viewed as
  \(<p_{s_1}, \text{Null}, \text{first–applicable}, \langle p_1, p_2 \rangle>\).

B. Turning XACML into ASP

We provide a translation module that turns an XACML description into a program in ASP. This interprets a formal semantics of XACML language in terms of the Answer Set semantics.

The translation module coverts an XACML rule
\(<\text{RuleID}, \text{Effect}, \text{Target}, \text{Condition}>\)

1\text{http://www.tcs.hut.fi/Software/smodels.}
2\text{http://www.cs.utexas.edu/users/tag/cmodels.html.}
3\text{http://potassco.sourceforge.net.}
into a set of ASP rules

\[ \text{decision}(\text{RuleID}, \text{Effect}) \leftarrow \text{Target} \land \text{Condition}. \]

An XACML policy

\[ \langle \text{PolicyID}, \text{Target}, \text{Combining Algorithm} \rangle, \langle r_1, \ldots, r_n \rangle \]

can be also translated into a set of ASP rules. In the following we assume that \( R \) and \( R' \) are variables that range over all rule ids, and \( V \) is a variable that ranges over \{permit, deny, indeterminate\}. In order to represent the effect of each rule \( r_i \) (\( 1 \leq i \leq n \)) on policy, we write

\[ \text{decision}(\text{PolicyID}, r_i, V) \leftarrow \text{decision}(r_i, V). \]

Each rule combining algorithms is turned into logic programming rules under the stable model semantics as follows:

- \textbf{permit–overrides} of policy \( p \) is represented as
  \[ \text{decision}(p, \text{permit}) \leftarrow \text{decision_from}(p, R, \text{permit}) \land \text{Target}. \]
  \[ \text{decision}(p, \text{deny}) \leftarrow \text{decision_from}(p, R, \text{deny}) \]
  \[ \land \neg \text{decision}(p, \text{permit}) \land \text{Target}. \]

- \textbf{deny–overrides} of policy \( p \) is represented as
  \[ \text{decision}(p, \text{deny}) \leftarrow \text{decision_from}(p, R, \text{deny}) \land \text{Target}. \]
  \[ \text{decision}(p, \text{permit}) \leftarrow \text{decision_from}(p, R, \text{permit}) \]
  \[ \land \neg \text{decision}(p, \text{deny}) \land \text{Target}. \]

- \textbf{first–applicable} of policy \( p \) is represented as
  \[ \text{has decision from}(p, R) \leftarrow \text{decision_from}(p, R, V). \]
  \[ \text{decision}(p, V) \leftarrow \text{decision_from}(p, r_i, V) \]
  \[ \land \bigwedge_{1 \leq k \leq i-1} \neg \text{has decision from}(p, r_k) \land \text{Target}. \]

The translation of a policy set is similar to the translation of a policy except that the policy combining algorithm only–one–applicable needs to be taken into account. For instance, only–one–applicable of policy set \( ps \) is represented as follows:

\[ \text{decision}(ps, V) \leftarrow \text{decision_from}(ps, P, V) \]
\[ \land \{ \text{has decision from}(ps, P) : \text{policy}(P) \} \}. \]
\[ \text{decision}(ps, \text{indeterminate}) \leftarrow \] 2 \{ \text{has decision from}(ps, P) : \text{policy}(P) \}. \]

Figure 4 shows an ASP representation of the example XACML policy in the language of GRINGO by applying our translation approach.

C. XACML Policy Analysis Using ASP

Once we represent an XACML into an ASP program \( \Pi \), we can use off-the-shelf ASP solvers for several automated analysis services. In this section, we mainly illustrate how policy verification can be handled by our policy analysis approach.

\[ \text{value}(\text{permit};\text{deny};\text{indeterminate}). \]
\[ \text{rule}(r_1;r_2;r_3;r_4;r_5). \]
\[ \text{policy}(p_1;p_2). \]
\[ \text{policyset}(ps_1). \]
\[ \text{time}(0..23). \]
\[ \#\text{domain value}(V;V_1). \]
\[ \#\text{domain rule}(R;R_1). \]
\[ \#\text{domain policy}(P). \]
\[ \#\text{domain time}(T). \]
\[ \%\text{domain definition} \]
\[ \text{subject}(\text{employee}) \leftarrow \text{subject} (\text{developer}). \]
\[ \text{subject}(\text{employee}) \leftarrow \text{subject} (\text{tester}). \]
\[ \% r_1 \]
\[ \text{decision}(r_1,\text{permit}) \leftarrow \text{subject} (\text{employee}), \text{action} (\text{read}), \text{resource}(\text{codes}), 8 < T, T < 17, \text{current_time}(T). \]
\[ \text{decision}(r_1,\text{permit}) \leftarrow \text{subject} (\text{developer}), \text{action} (\text{change}), \text{resource}(\text{codes}), 8 < T, T < 17, \text{current_time}(T). \]
\[ \% r_2 \]
\[ \text{decision}(r_2,\text{deny}) \leftarrow \text{subject} (\text{employee}), \text{action} (\text{change}), \text{resource}(\text{codes}). \]
\[ \text{decision}(r_2,\text{deny}) \leftarrow \text{subject} (\text{developer}), \text{action} (\text{read}), \text{resource}(\text{codes}). \]
\[ \text{decision}(r_2,\text{deny}) \leftarrow \text{subject} (\text{ tester}), \text{action} (\text{read}), \text{resource}(\text{codes}). \]
\[ \% r_3 \]
\[ \text{decision}(r_3,\text{permit}) \leftarrow \text{subject} (\text{developer}), \text{action} (\text{read}), \text{resource}(\text{codes}). \]
\[ \% r_4 \]
\[ \text{decision}(r_4,\text{deny}) \leftarrow \text{subject} (\text{ tester}), \text{action} (\text{read}), \text{resource}(\text{codes}). \]
\[ \% r_5 \]
\[ \text{decision}(r_5,\text{deny}) \leftarrow \text{subject} (\text{developer}), \text{action} (\text{change}), \text{resource}(\text{codes}). \]
\[ \% p_1 \]
\[ \text{decision_from}(p_1, r_1, V) \leftarrow \text{decision}(r_1, V). \]
\[ \text{decision_from}(p_1, r_2, V) \leftarrow \text{decision}(r_2, V). \]
\[ \text{decision_from}(p_1, R, \text{permit}) \leftarrow \text{decision}(r_1, V). \]
\[ \text{decision_from}(p_1, R, \text{deny}) \leftarrow \text{decision}(r_2, V). \]
\[ \text{decision_from}(p_1, R_1, \text{permit}) \leftarrow \text{decision}(r_1, V). \]
\[ \% p_2 \]
\[ \text{decision_from}(p_2, r_3, V) \leftarrow \text{decision}(r_3, V). \]
\[ \text{decision_from}(p_2, r_4, V) \leftarrow \text{decision}(r_4, V). \]
\[ \text{decision_from}(p_2, r_5, V) \leftarrow \text{decision}(r_5, V). \]
\[ \text{decision_from}(p_2, R, \text{deny}) \leftarrow \text{decision}(r_4, V). \]
\[ \text{decision_from}(p_2, R, \text{permit}) \leftarrow \text{decision}(r_5, V). \]
\[ \text{decision}(p_2, \text{deny}) \leftarrow \text{decision}(r_2, \text{deny}). \]
\[ \% p_3 \]
\[ \text{decision_from}(p_3, p_1, V) \leftarrow \text{decision}(p_1, V). \]
\[ \text{decision_from}(p_3, p_2, V) \leftarrow \text{decision}(p_2, V). \]
\[ \text{has decision from}(p_3, p_1) \leftarrow \text{decision}(p_1, p_2, V). \]
\[ \text{has decision from}(p_3, p_1) \leftarrow \text{decision}(p_1, p_2, V). \]

The problem of verifying a security property \( F \) against an XACML description can be cast into the problem of checking whether the program

\[ \Pi \cup \Pi_{\text{query}} \cup \Pi_{\text{config}} \]

has no answer sets, where \( \Pi \) is the program corresponding to the XACML specification, \( \Pi_{\text{query}} \) is the program corresponding to the program that encodes the negation of the property to check, and \( \Pi_{\text{config}} \) is the following program that generates arbitrary configurations.

\[ \text{subject attributes}(\text{developer};\text{ tester};\text{ employee}). \]
\[ \text{action attributes}(\text{read};\text{ change}). \]
\[ \text{resource attributes}(\text{codes}). \]
\[ 1 \{ \text{subject}(X) : \text{subject attributes}(X) \}. \]
\[ 1 \{ \text{action}(X) : \text{action attributes}(X) \}. \]
If no answer set is found, this implies that the property is verified. Otherwise, an answer set returned by an ASP solver serves as a counterexample that indicates why the description does not entail $F$. This helps the policy designer find out the design flaws in the policy specification.

For example, consider the example XACML policy shown in Figure 1. We need to ensure that a developer cannot change codes during non-working hours. The input query $\Pi_{query}$ can be represented as follows:

$$\Pi_{query} : \text{working_hours} : 8 \leq T, T < 17, \text{current_time}(T), \text{check} :- \text{decision}(ps1, \text{permit}), \text{subject}(\text{developer}), \text{action}(\text{change}), \text{resource}(\text{codes}), \text{not working_hours}.$$

Given the corresponding ASP program of ps1, the negation of the property, and $\Pi_{config}$, GRINGO and CLASP return no answer set from which we conclude that the property is held.

As another example, consider the query if a developer is always allowed to read codes during non-working hours. This query $\Pi_{query}$ can be represented as:

$$\Pi_{query} : \text{working_hours} : 8 \leq T, T < 17, \text{current_time}(T), \text{check} :- \text{decision}(ps1, \text{deny}), \text{subject}(\text{developer}), \text{action}(\text{read}), \text{resource}(\text{codes}), \text{not working_hours}.$$

A policy designer may intend that this property would follow based on the policy specification. However, the following answer set is found, which indicates a design flaw of the policy.

$$\{\text{subject}(\text{developer}) \text{ action}(\text{read}) \text{ action}(\text{change}) \text{ resource}(\text{codes}) \text{ decision}(ps1, \text{deny}) \text{ decision}(p1, \text{deny}) \text{ decision}(p2, \text{deny}) \text{ decision}(r2, \text{deny}) \text{ decision}(r3, \text{permit}) \text{ decision}(r4, \text{deny})\}$$

That is, a developer’s request to read the codes is denied if his request also includes changing the codes\(^5\). From this answer set, the policy designer finds that $p_2$, which is supposed to return permit, returns deny. It is because $r_5$ returns deny, and the combining algorithm of $p_2$ is deny-overrides.

In fact, the reason that $p_{s1}$ returns deny is because $p_1$ returns deny. Rule $r_1$ is not applicable since its condition is not satisfied and rule $r_2$ returns deny. Then, the policy designer realizes the flaw and could disallow the concurrency of two actions within a request. However, even after adding such a constraint, another answer set is found as follows:

$$\{\text{subject}(\text{developer}) \text{ subject}(\text{tester}) \text{ action}(\text{read}) \text{ resource}(\text{codes})\}$$

\(^5\)XACML supports multi-valued requests, which contains multiple id-value pairs in the subject, resource, or action attribute.

That is, when someone is both developer and tester, he cannot read codes during non-working hours since rule $r_4$ disallows it. In this answer set, $p_{s2}$ returns deny because $p_1$ is not applicable and $p_2$ returns deny. In turn, it is because $r_4$ returns deny. If we add a constraint disallowing a person to be both developer and tester roles simultaneously, the program returns no answer set as intended. Disallowing two conflicting roles to be assigned to the same user is called separation of duty (SoD) in role-based access control, which is discussed in the subsequent section.

IV. XACML-BASED RBAC POLICY ANALYSIS

A. A Policy Analysis Framework

As we discussed in Section I, the current XACML profile for RBAC [4] only supports elements and relations from core and hierarchical RBAC omitting constraints in RBAC. This section focuses on how XACML-based RBAC policies can be analyzed based on the approaches that we discussed in the previous sections while considering elements, relations and constraints in RBAC. To support the reasoning for XACML-based RBAC policy, we introduce a policy analysis framework shown in Figure 5. Our framework first transforms XACML-based representation of core and hierarchical RBAC to ASP-based RBAC representation. In addition, the policy designers can specify the RBAC constraints using a general constraint specification scheme derived from the NIST/ANSI RBAC standard [8], [1]. Those general constraint specifications are translated to ASP-based constraint specifications. Therefore, representing both RBAC system configuration (core and hierarchical RBAC) and RBAC constraints in ASP enables us to support rigorous analysis of constraints that are not addressed in the current XACML profile.

B. Core and Hierarchical RBAC Representation

RBAC models define sets of elements including a set of roles, a set of users, and a set of permissions, and relationships among users, roles and permissions. In XACML profile for RBAC, Role Assignment (Policy) or (PolicySet) defines which roles can be enabled or assigned to whom. Suppose that a user john is assigned to two roles tester
and seniorDeveloper in the software development company. We can translate those user-to-role assignments (ura) to ASP as follows:

\[
\text{ura}(\text{john}, \text{tester}). \\
\text{ura}(\text{john}, \text{seniorDeveloper}).
\]

RBAC supports role hierarchy relations. For example, developer is a junior role of seniorDeveloper in the software development company. The hierarchy relation between two roles developer and seniorDeveloper represented in XACML can be converted into ASP as follows:

\[
\text{junior}(\text{developer}, \text{seniorDeveloper}).
\]

In addition, we assume that relation junior is reflexive.

\[
\text{junior}(R, R) :- \text{rules}(R).
\]

\[
\text{tc}_\text{junior}(R1, R2) :- \text{junior}(R1, R2).
\]

Furthermore, the following definition is required to specify a user-to-role assignment considering the role hierarchy relations. It implies if a role \( r_2 \) is a junior role of \( r_1 \) and \( r_1 \) is assigned to a user \( u \), \( r_2 \) is also implicitly assigned to the user \( u \).

\[
\text{ura}(U, R2) :- \text{ura}(U, R1), \text{tc}_\text{junior}(R2, R1)
\]

Similarly, a session-to-role relation with respect to the role hierarchy relations is defined as follows:

\[
\text{sr}(S, R2) :- \text{sr}(S, R1), \text{tc}_\text{junior}(R2, R1)
\]

C. RBAC Constraint Representation

As part of RBAC constraints, we demonstrate how SoD constraints can be represented in ASP programs based on our framework. Most existing definitions of SoD constraints only consider a conflicting set as a pair of elements. For example, a constraint may declare a pair of conflicting roles \( r_1 \) and \( r_2 \), and require that no user is allowed to simultaneously assign to both \( r_1 \) and \( r_2 \). These definitions are too restrictive in the size of a conflicting set and the combination of elements in the set for which assignment operation is constrained. Thus, a more general example of SoD constraints should require that no user is allowed to be simultaneously assigned to \( n \) or more roles from a conflicting role set. In NIST/ANSI RBAC standard, SoD constraints are defined with two arguments: (a) a conflicting role set \( cr \) that includes two or more roles; and (b) a natural number \( n \), called the cardinality, with the property that \( 2 \leq n \leq |cr| \) means a user can be assigned to at most \( n \) roles from conflicting role set \( cr \). A similar definition is used in dynamic SoD constraints with respect to the activation of roles in sessions.

The NIST/ANSI RBAC standard has limitations in the constraint definitions. First, the conflicting notion is only applied to role without considering other components such as user and permission in RBAC. In the real world, we may also have notions of conflicting permissions or conflicting users based on the organizational policy. Second, historical SoD constraints are not addressed in RBAC standard. To address these issues, we provide a more general constraint specification method based on the RBAC standard.

**Definition 1: (SoD Constraint).** A SoD constraint is a tuple \( SoD = (t, e, cs, n) \), where

- \( t \in \{s, d, h\} \) represents the types of SoD constraints, where \( s \), \( d \) and \( h \) stand for static, dynamic and historical, respectively;
- \( e \in \{U, R, P\} \) is the RBAC element to which the constraint is applied, where \( U \), \( R \) and \( P \) denote User, Role and Permission, respectively;
- \( cs \) is the conflicting element set including conflict role set \( cr \), conflict user set \( cu \) and conflict permission set \( cp \); and
- \( n \) is an integer, such that \( 2 \leq n \leq |cs| \).

RBAC constraints defined by this general scheme can be used to construct ASP-based constraint specifications. A detailed construction algorithm is described in Algorithm 1. In this algorithm, three kinds of SoD constraints are supported depending on the value of \( t \) in a constraint specification. For static SoD constraints, if the value of \( e \) is \( R \), the algorithm further examines the types of conflicting element, which is either user or permission indicating user-centric or permission-centric constraints, respectively. Note that \( us \) indicates a user-to-session relation in this algorithm.

Next, we illustrate three typical RBAC constraints specified in our general scheme and give equivalent ASP expressions generated by our construction algorithm.

**Constraint 1: (SSoD-CR): The number of conflicting roles, which are from the same conflicting role set and authorized to a user, cannot exceed the cardinality of the conflicting role set.**

Suppose tester and developer belong to a static conflicting role set and the cardinality of the conflicting role set is two. That is, these roles cannot be assigned to the same user at the same time.

**Constraint Expression:**

\[ (s, U, \text{tester}, \text{developer}, 2) \]

**Constructed ASP Expression:**

\[ :- 2\{\text{ura}(U, \text{tester}), \text{ura}(U, \text{developer})\}. \]

**Constraint 2: (User-based DSoD): The number of conflicting roles, which are from the same conflicting role set and activated directly (or indirectly via inheritance) by a user, cannot exceed the cardinality of the conflicting role set.**

Assume tester and developer are contained in a dynamic conflicting role set and the cardinality of the conflicting role set is two. It means they are dynamic conflicting roles and cannot be activated by a user simultaneously.
Algorithm 1: Construction of ASP-based Constraint Expression

Input: A general constraint expression \( C \).
Output: An ASP constraint expression \( C' \).

1. \( C \leftarrow \{ \text{t, e, cs, n} \} \).
2. /* Static Constraint*/
3. if \( c.t = \text{s} \) then
4. if \( c.e = \text{U} \) then
5. foreach \( r \in c.e.cs \) do
6. \( \text{URA.append} (\text{ura}(\text{U}, r)) \);
7. \( C' \leftarrow \{ -c.e.n (\text{URA}) \} \);
8. if \( c.e = R' \) then
9. if \( \text{user} (c.cs) = \text{true} \) then
10. foreach \( a \in c.cs \) do
11. \( \text{URA.append} (\text{ura}(a, R)) \);
12. \( C' \leftarrow \{ -c.e.n (\text{URA}) \} \);
13. if \( \text{permission} (c.cs) = \text{true} \) then
14. foreach \( p \in c.cs \) do
15. \( \text{PRA.append} (\text{pra}(p, R)) \);
16. \( C' \leftarrow \{ -c.e.n (\text{PRA}) \} \);

17. /* Dynamic Constraint*/
18. if \( c.t = \text{d} \) then
19. \( i \leftarrow 0 \);
20. foreach \( r \in c.e.cs \) do
21. \( i \leftarrow i + 1 \);
22. \( \text{SR.append} (\text{sr} (\text{Si}, r)) \);
23. \( \text{US.append} (\text{us} (\text{U}, \text{Si})) \);
24. \( C' \leftarrow \{ -c.e.n (\text{SR}), \text{US} \} \);
25. /* Historical Constraint*/
26. if \( c.t = \text{h} \) then
27. \( i \leftarrow 0 \);
28. foreach \( r \in c.e.cs \) do
29. \( i \leftarrow i + 1 \);
30. \( \text{SR.append} (\text{sr} (\text{Si}, r, T)) \);
31. \( \text{US.append} (\text{us} (\text{U}, \text{Si}, T)) \);
32. \( C' \leftarrow \{ -c.e.n (\text{SR}), \text{US} \} \);
33. return \( C' \).

Constraint Expression:

\( \{ \text{d}, \text{U}, \text{tester, developer, 2} \} \)

Constructed ASP Expression:

\[ :- 2\{ \text{sr} (\text{S1, tester, T1}), \text{sr} (\text{S2, developer, T2}), \text{us} (\text{U, S1, T1}), \text{us} (\text{U, S2, T2}) \}. \]

Most of existing work in specifying \([3, 7, 17]\) and analyzing \([25, 27, 12]\) SoD constraints mainly focus on the system state at one point in time. By introducing a temporal variable \( \text{time} \) in ASP representation, the changing system state can be taken into account for both RBAC constraint specification and analysis in ASP representation.

Constraint 3: (Historical SoD): The number of activated roles from a conflicting role set by a user cannot exceed the cardinality of the historical conflicting role set.

Assume that two roles tester and developer are contained in a historical conflicting role set and the cardinality of the conflicting role set is two.

Constraint Expression:

\( \langle \text{h}, \text{U}, \text{tester, developer, 2} \rangle \)

Constructed ASP Expression:

\[ :- 2\{ \text{sr} (\text{S1, tester, T1}), \text{sr} (\text{S2, developer, T2}), \text{us} (\text{U, S1, T1}), \text{us} (\text{U, S2, T2}) \}. \]

Note that we introduce two time variables \( T1 \) and \( T2 \) to reflect the changing system states in this constraint representation. Thus, the constraint violations for the changing system state can be identified. For example, we can evaluate if a user ever activated two conflicting roles at different time intervals by checking the historical SoD constraints as a security property against the changing system states.

D. Violation Analysis of RBAC Constraints

![Constraint Example](image)

Figure 6. Violation checking for SoD constraints.

RBAC constraints can be utilized as security properties to check against access control policy configurations for identifying constraint violations. Figure 6 shows a typical example, which illustrates conflicting roles cannot be directly or indirectly (via inheritance) assigned to the same user. Figure 6 (a) shows that the user john is assigned to two roles tester and developer simultaneously. However, since tester is mutually exclusive to developer, the SSSoD-CR constraint is violated. Figure 6 (b) depicts a more complex example taking role hierarchy into account. The user john acquires two conflicting roles tester and developer through the permission inheritance. The SoD property supporting the role hierarchy can be specified with ASP as follows:

\[ \text{check} :- \text{ura} (\text{U}, \text{tester}), \text{ura} (\text{U}, \text{developer}). \]

If an answer set that is returned by an ASP solver contains check, it means that a user is assigned to two conflicting roles tester and developer in current RBAC configuration. Thus an SoD constraint violation is identified.
V. IMPLEMENTATION AND EVALUATION

We have implemented a tool called XACML2ASP in Java 1.6.3. XACML2ASP can automatically convert core XACML and RBAC constraint expressions into ASP. The generated ASP-based policy representations are then fed into an ASP reasoner to carry out analysis services. We evaluated the efficiency and effectiveness of our approach on several real-world XACML policies. GRINGO was employed as the ASP solver for our evaluation. Our experiments were performed on an Intel Core 2 Duo CPU 3.00 GHz with 3.25 GB RAM running on Windows XP SP2.

In our evaluation, we utilized ten real-world XACML policies collected from three different sources. Six of the policies, CodeA, CodeB, CodeC, CodeD, Continue-a and Continue-b are XACML policies used by [10]; among them, Continue-a and Continue-b are designed for a real-world Web application supporting a conference management. Three of the policies Weindx, FreeCS and GradeSheet are utilized by [5]. The Pluto policy is employed in ARCHON6 system, which is a digital library that federates the collections of physics with multiple degrees of meta data richness.

<table>
<thead>
<tr>
<th>Policy</th>
<th># of Rules</th>
<th>Converting Time(s)</th>
<th>Reasoning Time(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CodeA</td>
<td>2</td>
<td>0.000</td>
<td>0.000</td>
</tr>
<tr>
<td>CodeB</td>
<td>3</td>
<td>0.000</td>
<td>0.000</td>
</tr>
<tr>
<td>CodeC</td>
<td>4</td>
<td>0.000</td>
<td>0.002</td>
</tr>
<tr>
<td>CodeD</td>
<td>5</td>
<td>0.000</td>
<td>0.004</td>
</tr>
<tr>
<td>Weindx</td>
<td>6</td>
<td>0.005</td>
<td>0.006</td>
</tr>
<tr>
<td>FreeCS</td>
<td>7</td>
<td>0.005</td>
<td>0.006</td>
</tr>
<tr>
<td>GradeSheet</td>
<td>14</td>
<td>0.015</td>
<td>0.012</td>
</tr>
<tr>
<td>Pluto</td>
<td>21</td>
<td>0.016</td>
<td>0.031</td>
</tr>
<tr>
<td>Continue-a</td>
<td>298</td>
<td>0.120</td>
<td>0.405</td>
</tr>
<tr>
<td>Continue-b</td>
<td>306</td>
<td>0.125</td>
<td>0.427</td>
</tr>
</tbody>
</table>

Table I shows the number of rules contained in each policy, the conversion time from XACML to ASP, and the reasoning time using GRINGO + CLASPD for each policy. Note that the reasoning time was measured by enabling GRINGO + CLASPD to generate answer sets representing all permitted requests for each policy. From Table I, we observe that the conversion time from XACML to ASP in XACML2ASP is fast enough to handle larger size of policies, such as Continue-a and Continue-b. It also indicates that the reasoning process for policy analysis in ASP solver is also efficient enough for a variety of policy analysis services.

VI. RELATED WORK

In [13], a framework for automated verification of access control policies based on relational first-order logic was proposed. The authors demonstrated how XACML policies can be translated to the Alloy language [14], and checked their security properties using the Alloy Analyzer. However, using the first-order constructs of Alloy to model XACML policies is expensive and still needs to examine its feasibility for larger size of policies. In [6], the authors formalized XACML policies using a process algebra known as Communicating Sequential Processes. This utilizes a model checker to formally verify properties of policies, and to compare access control policies with each other. Fisler et al. [10] introduced an approach to represent XACML policies with Multi-Terminal Binary Decision Diagrams (MTBDDs). A policy analysis tool called Margrave was developed. Margrave can verify XACML policies against the given properties and perform change-impact analysis based on the semantic differences between the MTBDDs representing the policies. Kolovski et al. [16] presented a formalization of XACML using description logic (DL), which is a family of languages that are decidable subsets of first-order logic, and leveraged existing DL reasoners to conduct policy verification. Compared with other work in XACML, our approach provides a more straightforward formalization with ASP addressing XACML features such as all four combining algorithms and handling simple conditions.

Schaad and Moffett [25] specified the access control policies under the RBAC96 and ARBAC97 models and a set of separation of duty constraints in Alloy. They attempted to check the constraint violations caused by administrative operations. In [26], Sohr et al. demonstrated how the USE tool, a validation tool for OCL constraints, can be utilized to validate authorization constraints against RBAC configurations. The policy designers can employ the USE-based approach to detect certain conflicts between authorization constraints and to identify missing constraints. Assurance Management Framework (AMF) was proposed in [2], [12], where formal RBAC model and constraints can be analyzed. Alloy was also utilized as an underlying formal verification tool to analyze the formal specifications of an RBAC model and corresponding constraints, which are then used for access control system development. In addition, the verified specifications are used to automatically derive the test cases for conformance testing. Even though there has been a great amount of work on XACML and RBAC analysis, there is little work in providing reasoning in XACML-based RBAC policies.

VII. CONCLUSION AND FUTURE WORK

In this work, we have provided a formal foundation of XACML in terms of ASP. Also, we further introduced a policy analysis framework for identifying constraint violations in XACML-based RBAC policies, explicitly demonstrating existing XACML standard does not support the constrained RBAC. In addition, we have described a tool called XACML2ASP, which can seamlessly work with existing ASP solvers for XACML policy analysis. Our experiments showed that the performance of our analysis approach could efficiently support larger access control policies.
For our future work, the coverage of our mapping approach needs to be further extended with more XACML features such as handling complicated conditions, obligation and other attribute functions. Also, it is necessary to enhance our tool to provide those features and corresponding analysis services while obscuring the details of the ASP formalism.

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REFERENCES